# Stanton Community Primary School

Nurture, Enjoy, Aspire, Achieve



# Mathematics Calculation Policy

<u>Contents</u> Introduction to Mathematics Mastery Resources for Teaching Mathematics Objective Overviews Strategies used for teaching of Mastery Mathematics Mathematical Language

# Teaching for Mathematics Mastery

At Stanton Primary School, we believe that every child has the potential to succeed, having access to the same curriculum content as their peers, and acquiring a deep, long---term, secure and adaptable understanding of the subject. Think of it like a game of Jenga; if children learn by rote, and speed through concepts without learning them in depth, eventually, when they reach the top, there will be so many pieces missing that the foundation will not be stable and gaps will have developed in their understanding. At Stanton, all teachers use the White Rose Maths Hub as a process for teaching mathematics. When introducing children to new concepts, they should have the opportunity to build fluency in topics by taking the following approach:

**Concrete** – children should have the opportunity to use concrete objects and manipulatives to help them understand what they are doing.

**Pictorial** – children should build on this concrete approach by using pictorial representations. These representations can then be used to reason and solve problems.

**Abstract** – with the foundations firmly laid, children should be able to move to an abstract approach using numbers and key concepts with confidence.

Reasoning and problem solving is encompassed in the above approaches to deepen and master all aspects of mathematics. This policy outlines the different calculation strategies that should be taught and used from Year R to Year 6 in line with the requirements of the 2014 Primary National Curriculum, giving examples of concrete, pictorial and abstract calculations.

# **Resources for Teaching Mathematics**

Teachers can use any teaching resources that they wish to use and the policy does not recommend one set of resources over another, rather that, a variety of resources are used. For each of the four rules of number, different strategies are laid out, together with examples of what concrete materials can be used and how, along with suggested pictorial representations. The principle of the concrete---pictorial---abstract (CPA) approach [Make it, Draw it, Write it] is for children to have a true understanding of a mathematical concept they need to master all three phases. At Stanton Primary School, the following concrete objects are available for all children to use:



Diennes (Base 10)	
Cuisenaires (Bar Method)	
Place Value Counters	



	Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Addition	Recites numbers in order to 10. Knows that numbers identify how many objects are in a set. Beginning to represent numbers using fingers, marks on paper or pictures. Sometimes matches numeral and quantity correctly. Compares two groups of objects, saying when they have the same number. Shows an interest in number problems. Separates a group of three or four objects in different ways, beginning to recognise that the total is still the same. Shows an interest in numerals in the environment. Shows an interest in numerals in the environment. Shows an interest in numerals in the environment. Shows an interest in numerals in the vironment. Shows an interest in numerals in the vironment. Shows an interest in numerals in the environment. Shows an interest in numerals in the vironment.	Children count reliably with numbers from one to 10, place them in order and say which number is one more or one less than a given number. Using quantities and objects, they add and subtract two single-digit numbers and count on or back to find the answer. They solve problems, including doubling, halving and sharing.	parts top make a whole; part whole model Starting at the bigger number and counting on	<ul> <li>Adding three single digits</li> <li>Column method - no regrouping</li> </ul>	Column methods regrouping (up to 3 digits)	<ul> <li>Column methods regrouping (up to 4 digits)</li> </ul>	<ul> <li>Column methods regrouping (up to 5 digits)</li> <li>Decimals with the same amount of decimal places</li> </ul>	<ul> <li>Column methods regrouping</li> <li>Decimals with different amount of decimal places</li> </ul>
Subtraction	many objects are in a set. sing fingers, marks on paper or pictures. quantity correctly. saying when they have the same number. lems. ur objects in different ways, beginning to rec he environment. 1 numbers. thing can be counted, including steps, claps o	count reliably with numbers from one to 10, place them in order and s than a given number. Intities and objects, they add and subtract two single-digit numbers in the problems, including doubling, halving and sharing.	Taking ones away Counting back Find the difference Find the whole	<ul> <li>Counting back</li> <li>Find the difference</li> <li>Part whole model</li> <li>Make 10</li> <li>Column method - no regrouping</li> </ul>	<ul> <li>Column methods regrouping (up to 3 digits)</li> </ul>	Column methods regrouping (up to 4 digits)	<ul> <li>Column methods regrouping (up to 5 digits)</li> <li>Decimals with the same amount of decimal places</li> </ul>	<ul> <li>Column methods regrouping</li> <li>Decimals with different amount of decimal places</li> </ul>
Multiplication	Recites numbers in order to 10. Knows that numbers identify how many objects are in a set. Beginning to represent numbers using fingers, marks on paper Sometimes matches numeral and quantity correctly. Compares two groups of objects, saying when they have the sc Shows an interest in number problems. Separates a group of three or four objects in different ways, same. Shows an interest in numerals in the environment. Shows an interest in representing numbers. Realises not only objects, but anything can be counted, includi	ren count reliably with numbers from one to 10, place tess than a given number. A quantities and objects, they add and subtract two singer. er. solve problems, including doubling, halving and sharing.	Counting in multiples	<ul> <li>Doubling</li> <li>Counting in multiples</li> <li>Repeated addition</li> <li>Arrays - showing commutativity</li> </ul>	<ul> <li>Counting in multiples</li> <li>Repeated addition</li> <li>Arrays - showing commutativity</li> <li>Grid method</li> </ul>	<ul> <li>Column multiplication (2 and 3 digits multiplied by 1 digit)</li> </ul>	<ul> <li>Column multiplication (up to 4 digits multiplied by 1 or 2 digits)</li> </ul>	<ul> <li>Column multiplication (up to 4 digits multiplied by 2 digits)</li> </ul>
Division	<ul> <li>Recites numbers in order to 10.</li> <li>Knows that numbers identify how many</li> <li>Beginning to represent numbers using f</li> <li>Sometimes matches numeral and quanti</li> <li>Compares two groups of objects, saying</li> <li>Shows an interest in number problems.</li> <li>Separates a group of three or four obj same.</li> <li>Shows an interest in numerals in the en same.</li> <li>Shows an interest in numerals in the en same.</li> <li>Rows an interest in numerals in the en same.</li> </ul>	<ul> <li>Children count reliably with n one less than a given number.</li> <li>Using quantities and objects, answer.</li> <li>They solve problems, includin</li> </ul>	objects into groups	<ul> <li>Division as grouping</li> <li>Division as arrays</li> </ul>		<ul> <li>Division within arrays</li> <li>Division with a remainder</li> <li>Short division (up to 3 digits by 1 digit)</li> </ul>	<ul> <li>Short division (up to 4 digit by 1 digit number)</li> <li>Interpret remainders in context</li> </ul>	<ul> <li>Short division</li> <li>Long division</li> <li>Interpret remainders as whole numbers, fractions or rounded.</li> </ul>

#### Addition





### Subtraction

Objective and Strategies	Concrete	Pictorial	Abstract
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. 6 - 2 = 4	Cross out drawn objects to show what has been taken away. $ \begin{array}{c}  & & & & & & \\  & & & & & & \\  & & & & $	18 -3= 15 8 - 2 = 6
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 - 4 Use counters and move them away from the group as you take them away counting backwards as you go.	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line. -10 -10 -10 -10 -10 -10 This can progress all the way to counting back using two 2 digit numbers.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.
Find the difference	Compare amounts and objects to find the difference. Use cubes to build towers or make bars to find the difference	+6 Count on to find the difference. 0 1 2 3 4 5 6 7 8 9 10 11 12 Comparison Bar Models Draw bars to find the difference between 2 numbers. 13 7 Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them. 13 7 Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them. 22	Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches.

Part Part Whole Model	Link to addition- use the part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is one of the parts. What is the other part? <b>10 - 6 =</b>	Use a pictorial representation of objects to show the part part whole model.	5 10 Move to using numbers within the part whole model.
Make 10	14-9=	13 - 7 = 6 $3 4$ $5 + 2 + 3 + 5 + 6 + 7 + 5 + 6 + 7 + 5 + 6 + 7 + 5 + 6 + 7 + 5 + 6 + 7 + 5 + 6 + 7 + 16 + 19 + 20$	16 - 8=
MAKE 10	Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.	Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	How many do we take off to reach the next 10? How many do we have left to take off?
Column method without regrouping	Ture       One         Use Base 10 to make the bigger number then take the smaller number away.         Use Base 10 to make the bigger number then take the smaller number away.         Use Base 10 to make the bigger number then take the smaller number away.         Use Base 10 to make the bigger number then take the smaller number away.         Use Base 10 to make the bigger number then take the smaller number away.         Use Base 10 to make the bigger number then take the smaller number away.         Use Base 10 to make the bigger number away.         Use Base 10 to make the larger number first.	Draw the Base 10 or place value counters alongside the written calculation to help to show working.	$47 - 24 = 23$ $-\frac{40 + 7}{20 + 3}$ This will lead to a clear written column subtraction. $32$ $-12$ $20$
Column method with regrouping	Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges. Make the larger number with the place value counters	Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.	836-254=582 $300-130-6$ $- 200-50-4$ $500-80-2$ Children can start their formal written method by partitioning the number into clear place value columns.



### Multiplication

<b>Objective and Strategies</b>	Concrete	Pictorial	Abstract
Doubling	Use practical activities to show how to double a number.	Draw pictures to show how to double a number. Double 4 is 8	16 16 10 10 10 10 10 10 10 12 Partition a number and then double each part before recombining it back together.
Counting in multiples		Use a number line or pictures to continue support in counting in	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30
Repeated addition	Count in multiples supported by concrete objects in equal groups.	multiples. There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 2 add 2 add 2 equals 6 5 + 5 + 5 = 15 5 + 5 + 5 = 15	Write addition sentences to describe objects and pictures. Write addition sentences to describe objects and pictures. 2 + 2 + 2 + 2 + 2 = 10
Arrays- showing commutative multiplication	Create arrays using counters/ cubes to show multiplication sentences.	Draw arrays in different rotations to find commutative multiplication sentences. 4 × 2 = 8 2 × 4 = 8 2 × 4 = 8 2 × 4 = 8 4 × 2 = 8	Use an array to write multiplication sentences and reinforce repeated addition.





## Division

Objective and Strategies	Concrete	Pictorial	Abstract
Sharing objects into groups	Image: Constraint of the second se	Children use pictures or shapes to share quantities. $ \begin{array}{c}  & & & & & \\  & & & & & \\  & & & & & \\  & & & &$	Share 9 buns between three people. 9 ÷ 3 = 3
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding. 96 + 3 = 32 96 + 3 =	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 3 3 3 3 3 3 Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group. 20 20 + 5 = ? 5 x ? = 20	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?
Division within arrays	E.g. 15 + 3 = 5       5 x 3 = 15       15 + 5 = 3       3 x 5 = 15	Draw an array and use lines to split the array into groups to make multiplication and division sentences.	Find the inverse of multiplication and division sentences by creating four linking number sentences. $7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$



Long division		$432 \div 15 \text{ becomes}$ $2  8 \cdot 8$ $1  5  4  3  2 \cdot 0$ $3  0  \psi$ $1  3  2$ $1  2  0$ $1  2  0$ $1  2  0$
		1 2 0 1 2 0 0

The 2014 National Curriculum is explicit in articulating the importance of children using the correct mathematical language as a central part of their learning (reasoning). Indeed, in certain year groups, the non---statutory guidance highlights the requirement for children to extend their language around certain concepts. It is therefore essential that teaching using the strategies outlined in this policy is accompanied by the use of appropriate and precise mathematical vocabulary.

New vocabulary should be introduced in a suitable context (for example, with relevant real objects, apparatus, pictures or diagrams) and explained carefully. High expectations of the mathematical language used are essential, with teachers only accepting what is correct.

Correct Terminology	Old Terminology (no longer used)
ones	units
is equal to (is the same as)	equals
zero	Oh (the letter o)
exchange	Stealing
exchanging	borrowing
regrouping	
calculation	Generic term of 'sum' or 'number sentence'
equation	

## Glossary

Concept	Definition
Acute	Describes angles between 0 and 90 degrees.
Adjacent	Adjoining (as used to describe lines and angles).
Alternate	Every other one in a sequence.
Angle	The number of degrees rotated around a point.
Area	The amount of space within a perimeter (expressed in square units).
Ascending order	The arrangement of numbers from smallest to largest.
Average	A number representing a set of numbers (obtained by dividing the total of
	the numbers by the numbers itself).
Axis of symmetry	A line dividing a shape into two symmetrical parts.

Concept	Definition
Baker's dozen	The colloquial name given to the number 13.
Base	The line or face on which a shape is standing.
Base angles	Those angles adjacent to the base of a shape.
Bisect	To divide into two equal parts.
Breadth	Breadth is another name for width. It is the distance across from side to
Breadth	side.

Concept	Definition
Capacity	The amount of space in an object (the amount of liquid or air it contains).
Cardinal number	A number that shows quantity but not order.
Carroll Diagram	A number that shows quantity but not order.
Circumference	The distance around a circle (its perimeter).
Composite number	A number with more than two factors.
Congruent	Congruent shapes are the same shape and size (equal).
Consecutive	Consecutive numbers follow in order without interruption (e.g. 2,3,4,5).
Coordinates	Numbers used to locate a point on a grid.

Concept	Definition
Denominator	The number below the line in a fraction.
Descending order	The arrangement of numbers from the largest to smallest.
Diagonal	A straight line connecting two non- adjacent vertices (corners) of a polygon.
Difference	By how much a number is bigger or smaller than another.
Digit	Any number from 0 to 9 (inclusive).
Digital root	The digital root of 58 is 4 because $5 + 8 = 13$ and $1 + 3 = 4$
Dimensions	The measurements of a shape (i.e. length, width, height).
Dodecagon	A twelve sided polygon.

Concept	Definition
Edge	The intersection of two faces of a three-dimensional object.
Equation	A statement of equality between two expressions (e.g. $3 \times 4 = 6 + 6$ ).
Equilateral triangle	A triangle with congruent (equal) sides and angles.
Even number	A positive or negative number exactly divisible by 2.
Exterior	Outside.

Concept	Definition
Face	A plane surface of a three-dimensional object.
Face value	The numeral itself despite its position in a number (e.g. the face value of 8 in 38,250 is 8).
Factor	A number which will divide exactly into another number.

Concept	Definition
Greater than	An inequality between numbers. The symbol used to represent greater
	than is an arrow pointing towards the smallest number.
Gross	The name given to the number 144.

Concept	Definition
Hendecagon	A two dimensional shape with eleven sides and eleven angles also called an
	undecagon.
Heptagon	A two dimensional shape with seven sides and seven angles also called a
	septagon.
Hexagon	A polygon with six sides.
Horizontal	Describes a line or plane parallel to the earth's surface.

Concept	Definition
Improper fraction	A fraction whose numerator is equal to or greater than it denominator.
Integer	A negative or positive whole number.
Interior	Inside.
Intersection	The point or line where two lines or two faces meet.
Irregular shapes	Shapes which do not have all congruent sides and all congruent angles.
Isosceles triangle	A triangle which has two equal sides of equal length.

Concept	Definition
Kite	A quadrilateral that has two adjacent pairs of sides that are equal in length,
	and at least one pair of opposite angles are equal.

Concept	Definition
Less than	An inequality between numbers. The symbol used to represent less than is
	an arrow pointing towards the smallest number.
Lozenge	Another name for a rhombus.

Concept	Definition
Mean	The average of a set of numbers. The sum of the values in a set of data
	divided by the total number of items in that set.
Median	The middle value of a set of ordered data.
Mode	The value that occurs the most often in a set of data
Multiple	The product of a given number with another factor.

Concept	Definition
Numerator	The number above the line in a fraction.

Concept	Definition
Oblique	Oblique means sloping or slanting.
Oblong	A shape with two pairs of straight, unequal sides and four right angles. Also
	known as a rectangle.
Obtuse angle	An angle between 90 and 180 degrees.
Octagon	A polygon with eight sides and eight angles.
Odd number	A number that when divided by two leaves a remainder of one.
Ordinal number	Describes a position in a number sequence.

Concept	Definition
Parallel lines	Lines with no common points and always the same distance apart.
Parallelogram	A four-sided polygon with opposite sides equal and parallel and the opposite angles are equal in size.
Perimeter	The length of the distance around the boundary of a shape.
Perpendicular line	A line at right angles to another line or plane.
Polyhedron	A three dimensional shape with plane faces.
Place value	Indicates the position of a numeral (e.g. the place value of the 3 in 738 is 30)
Prime number	A number with only two factors, 1 and itself (e.g. 2,3,5,7,11, 13, 17, 19, 23)
Product	The result when two or more numbers are multiplied.

Concept	Definition
Quadrant	A quarter of the area of a circle which also contains a right angle.
Quotient	The result when one number is divided by another number.
Quindecagon	A polygon with fifteen sides and fifteen angles.

Concept	Definition
Rectangle	A quadrilateral with opposite sides equal and parallel and containing four right angles
Reflex angle	An angle greater than 180 degrees.
Rhombus	A parallelogram with congruent sides. Opposite sides are parallel and
	opposite sides are equal in size.
Roman numerals	Seven letters are used in combination to write numbers:
	I = 1 V = 5 X = 10 L = 50 C = 100 D = 500 M = 1000
Rotational symmetry	A shape is said to have rotational symmetry if it looks the same in different
	positions when rotated about its centre.
Rounding	An approximation used to express a number in a more convenient way.

Concept	Definition
Scalene triangle	A triangle that has three sides of different length and no equal angles.
Score	The name given to the number 20.
Squared	A number squared is a number multiplied by itself.
Courses number	A number whose units can be arranged into a square (e.g.
Square number	1,4,9,16,25,36,49,64)
Sum	The result when two or more numbers are added together.
Summetrical	A shape is symmetrical if it is identical on either side of a line dividing it into
Symmetrical	two parts.

Concept	Definition
Tally	A record of items using vertical and oblique lines to represent each item.
Tetragon	A four sided shape.
Tessellation	Shapes fitted together with a number of exact copies and with no overlaps
ressenation	or gaps.
Translation	This takes place when a shape is moved from one place to another just by
Taisiation	sliding it (without rotating, reflecting or enlarging).
Trapezium	A quadrilateral with two parallel sides.
Triangular number	A number whose units can be arranged into a triangle (e.g. 1, 3, 6, 10, 15,
	21)
Trigon	A three sided shape.

Concept	Definition
Vertex	The point at which two or more line segments or two or more edges of a polyhedron meet.
Vertical line	A line which is at right angles to a horizontal line.